

DESCENT SPECTRAL VERSIONS OF THE TRADITIONAL CONJUGATE GRADIENT ALGORITHMS WITH APPLICATION TO NONNEGATIVE MATRIX FACTORIZATION

Fatemeh DARGAHI¹, Saman BABAIE-KAFAKI²,
Zohre AMINIFARD³

***Abstract.** Despite computational superiorities, some traditional conjugate gradient algorithms such as Polak–Ribière–Polyak and Hestenes–Stiefel methods generally fail to guarantee the descent condition. Here, in a matrix viewpoint, spectral versions of such methods are developed which fulfill the descent condition. The convergence of the given spectral algorithms is argued briefly. Afterwards, we propose an improved version of the nonnegative matrix factorization problem by adding penalty terms to the model, for controlling the condition number of one of the factorization elements. Finally, the computational merits of the method are examined using a set of CUTer test problems as well as some random nonnegative matrix factorization models. The results typically agree with our analytical spectrum.*

Keywords: Unconstrained optimization, conjugate gradient method, spectral method, rank-one update, nonnegative matrix factorization.

DOI [10.56082/annalsarsciinfo.2024.1.35](https://doi.org/10.56082/annalsarsciinfo.2024.1.35)

1. Introduction

Scholar studies show that the introduction of conjugate gradient (CG) methods made a revolution in the field of numerical optimization. Requiring low memory and having simple iterations besides acceptable convergence, the methods have been extensively utilized in practical disciplines such as signal processing, machine learning, and neural networks training, which often appear in large-scale models.

For solving the minimization problem $\min_{x \in \mathbb{R}^n} f(x)$ with a smooth real-valued function f , here we focus on the CG methods which their search directions can be formulated by

¹ PhD student, Department of Mathematics, “Semnan University”, Semnan, Iran, (fatemehdargahi@semnan.ac.ir).

² Prof., Department of Mathematics, “Semnan University”, Semnan, Iran, (sbk@semnan.ac.ir).

³ Senior Researcher, Department of Mathematics, “Semnan University”, Semnan, Iran (aminisor@semnan.ac.ir).
